

## 5 Percentages and uncertainty

A percentage is simply a fraction expressed as a decimal. It is important to be able to calculate routinely, but is often incorrectly calculated in exams. These pages should allow you to practise this skill.

### 5.1 Calculating percentages as proportions

To work out a percentage, you must identify or calculate the total number using the equation:

$$\text{percentage} = \frac{\text{number you want as a percentage of total number}}{\text{total number}} \times 100\%$$

For example, in a population, the number of people who have brown hair was counted.

The results showed that in the total population of 4600 people, 1800 people had brown hair.

The percentage of people with brown hair is found by calculating:

$$\begin{aligned} & \frac{\text{number of people with brown hair}}{\text{total number of people}} \times 100 \\ & = \frac{1800}{4600} \times 100 = 39.1\% \end{aligned}$$

### Practice questions

- 1 The table below shows some data about energy absorbed by a tree in a year and how some of it is transferred.

Energy absorbed by the tree in a year	3 600 000 kJ/m <sup>2</sup>
Energy transferred to primary consumers	2240 kJ/m <sup>2</sup>
Energy transferred to secondary consumers	480 kJ/m <sup>2</sup>

Calculate the percentage of energy absorbed by the tree that is transferred to  
**a** primary consumers                      **b** secondary consumers.

- 2 One in 17 people in the UK has diabetes.  
 Calculate the percentage of the UK population that have diabetes.

### 5.2 Calculating the percentage change

When you work out an increase or a decrease as a percentage change, you must identify, or calculate, the total original amount:

$$\% \text{ increase} = \frac{\text{increase}}{\text{original amount}} \times 100$$

$$\% \text{ decrease} = \frac{\text{decrease}}{\text{original amount}} \times 100$$

**Remember:** When you calculate a percentage change, use the total *before* the increase or decrease, not the final total.

**Practice questions**

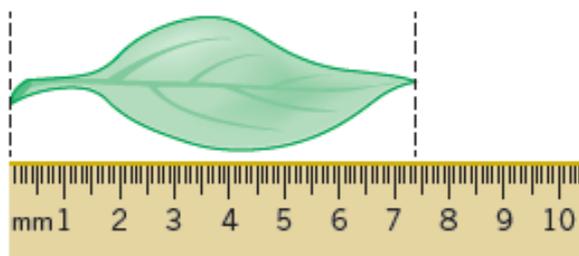
3 Convert the following mass changes as percentage changes.

Sucrose conc. / $\text{mol dm}^{-3}$	Initial mass / g	Final mass / g	Mass change / g	Percentage change in mass
0.9	1.79	1.06		
0.7	1.86	1.30		
0.5	1.95	1.70		
0.3	1.63	1.76		
0.1	1.82	2.55		

**5.3 Measurement uncertainties**

When you measure something, there will always be a small difference between the measured value and the true value. This may be because of the size of the scale divisions on your measuring equipment, or the difficulty of taking the measurement. This is called an uncertainty.

To estimate the uncertainty of a measurement with an instrument with a marked scale such as a ruler, a good rule of thumb is to let the uncertainty be equal to half the smallest division on the scale being used.



Using a ruler with a mm scale, the length of the leaf seems to be 74 mm. The smallest division is 1 mm, so the uncertainty is 0.5 mm.

The true length is therefore 74 mm  $\pm$  0.5 mm.

**Practice question**

4 Give the uncertainty for the following pieces of equipment:

- a large measuring cylinder with 2  $\text{cm}^3$  divisions
- digital stopwatch timer measuring to the nearest hundredth of a second
- thermometer with 0.1  $^{\circ}\text{C}$  divisions.

**5.4 Calculating percentage uncertainties**

The uncertainty is the range of possible error either side of the true value due to the scale being used, so the value recorded for the measurement = closest estimate  $\pm$  uncertainty.

The difference between the true value and the maximum or minimum value is called the **absolute error**.

Once the absolute error has been established for a particular measurement, it is possible to express this as a percentage uncertainty or **relative error**. The calculation to use is:

$$\text{relative error} = \frac{\text{absolute error}}{\text{measured value}} \times 100\%$$

In the leaf example above, the absolute error is  $\pm 0.5$  mm.

The relative error is therefore:

$$0.5/74 \times 100\% = 0.7\%$$

### Practice questions

5 Complete the table to show the missing values in the last two columns.

Measurement made	Equipment used	Absolute error	Relative error
Length of a fluid column in a respirometer is 6 mm	mm scale	0.5 mm	
Volume of a syringe is 12 cm <sup>3</sup> of liquid	0.5 cm <sup>3</sup> divisions		
Change in mass of 1.6 g	balance with 2 d.p.		

