

5 Work done, power, and efficiency

5.1 Work done

Work is done when energy is transferred. Work is done when a force makes something move. If work is done *by* an object its energy decreases and if work is done *on* an object its energy increases.

$$\text{work done} = \text{energy transferred} = \text{force} \times \text{distance}$$

Work and energy are measured in joules (J) and are scalar quantities (see Topic 3.1).

Practice question

- 1 Calculate the work done when the resultant force on a car is 22 kN and it travels 2.0 km.
- 1 Calculate the distance travelled when 62.5 kJ of work is done applying a force of 500 N to an object.

5.2 Power

Power is the rate of work done.

It is measured in watts (W) where 1 watt = 1 joule per second.

$$\text{power} = \frac{\text{energy transferred}}{\text{time taken}} \quad \text{or} \quad \text{power} = \frac{\text{work done}}{\text{time taken}}$$

$$P = \Delta W / \Delta t \quad \Delta \text{ is the symbol 'delta' and is used to mean a 'change in'}$$

Look at this worked example, which uses the equation for potential energy gained.

A motor lifts a mass m of 12 kg through a height Δh of 25 m in 6.0 s.

Gravitational potential energy gained:

$$\Delta PE = mg\Delta h = (12 \text{ kg}) \times (9.81 \text{ m s}^{-2}) \times (25 \text{ m}) = 2943 \text{ J}$$

$$\text{Power} = \frac{2943 \text{ J}}{6.0 \text{ s}} = 490 \text{ W (2 s.f.)}$$

Practice questions

- 2 Calculate the power of a crane motor that lifts a weight of 260 000 N through 25 m in 48 s.
- 3 A motor rated at 8.0 kW lifts a 2500 N load 15 m in 5.0 s. Calculate the output power.

5.3 Efficiency

Whenever work is done, energy is transferred and some energy is transferred to other forms, for example, heat or sound. The efficiency is a measure of how much of the energy is transferred usefully.

Efficiency is a ratio and is given as a decimal fraction between 0 (all the energy is wasted) and 1 (all the energy is usefully transferred) or as a percentage between 0 and 100%. It is not possible for anything to be 100% efficient: some energy is always lost to the surroundings.

$$\text{Efficiency} = \frac{\text{useful energy output}}{\text{total energy input}} \quad \text{or} \quad \text{Efficiency} = \frac{\text{useful power output}}{\text{total power input}}$$

(multiply by 100% for a percentage)

Look at this worked example.

A thermal power station uses 11 600 kWh of energy from fuel to generate electricity. A total of 4500 kWh of energy is output as electricity. Calculate the percentage of energy 'wasted' (dissipated in heating the surroundings).

You must calculate the energy wasted using the value for useful energy output:

$$\text{percentage energy wasted} = \frac{(\text{total energy input} - \text{energy output as electricity})}{\text{total energy input}} \times 100$$

$$\text{percentage energy wasted} = \frac{(11600 - 4500)}{11600} \times 100 = 61.2\% = 61\% \text{ (2 s.f.)}$$

Practice questions

- Calculate the percentage efficiency of a motor that does 8400 J of work to lift a load.
The electrical energy supplied is 11 200 J.
- An 850 W microwave oven has a power consumption of 1.2 kW.
Calculate the efficiency, as a percentage.
- Use your answer to question 4 above to calculate the percentage efficiency of the motor.
(The motor, rated at 8.0 kW, lifts a 2500 N load 15 m in 5.0 s.)
- Determine the time it takes for a 92% efficient 55 W electric motor take to lift a 15 N weight 2.5 m.